

- These standards are age-related expectations and therefore we expect the majority of children to achieve them.
- New learning is likely to be taught to groups rather than the whole class to acknowledge the different learning stages of the children.
- Children need to understand that division can be sharing or grouping (repeated subtraction).
- Children should understand that, unlike multiplication, division is **not** commutative.
- Ensure that children understand the = sign means is the same as, not makes, and that children see calculations where the equals sign is in a different position, e.g. $12 \div 3 = 4$ and $4 = 12 \div 3$.
- Children should be encouraged to approximate before calculating and check whether their answer is reasonable.

EARLY YEARS:

Children are encouraged to develop a mental picture of the number system in their heads to use for calculation. They should experience practical calculation opportunities involving equal groups and sharing items using a wide variety of equipment, e.g. small world play, role play, counters, cubes etc. They develop ways of recording calculations using pictures, etc.

End of Year 1 Expectations

Division: Pre-Stage 1

Pictures and marks.

12 children get into teams of 4 to play a game.
How many teams are there?



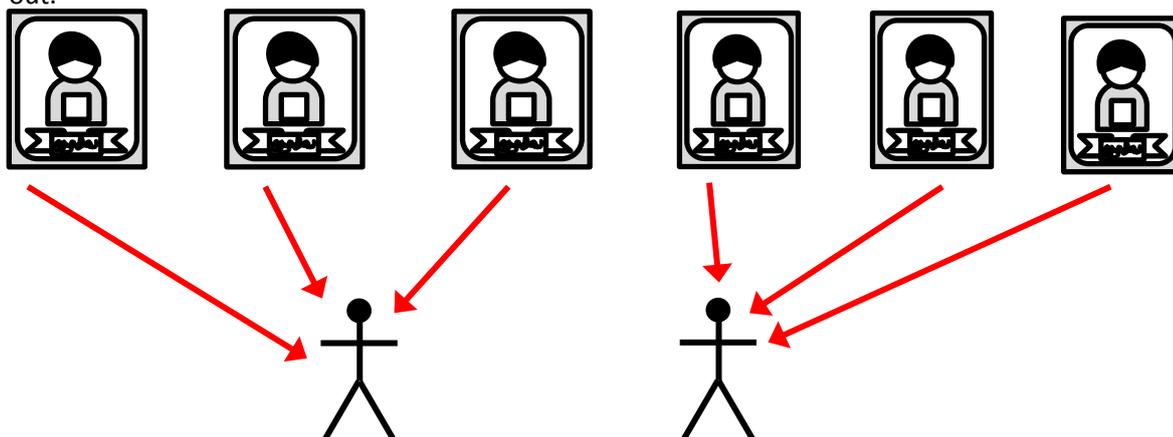


END OF YEAR 1 EXPECTATIONS:

In problem solving contexts, children will use practical equipment to share out objects equally and to group objects to represent division.

6 football stickers are shared between 2 people, how many do they each get?

Children may solve this by using a 'one for you, one for me' strategy until all of the cards have been given out.





Mathematics Calculation Guidelines

Progression through Calculations for DIVISION

Children should find the answer by counting how many cards **1 person** has got.
There are 6 football stickers, how many people can have 2 stickers each?



Children should find the answer by counting how many **groups of 2** there are.

The teacher can model the link between sharing and grouping in the following way by relating back to the first football sticker question:

Placing the football stickers in a bag or box, the teacher can ask the children how many stickers would need to be taken out of the box to give each person one sticker each (i.e. 2) and exemplify this by putting the cards in groups of 2 until all cards have been removed from the bag.

End of Year 2 Expectations

Division: Stage 1.

Sharing – 6 apples are shared between 2 people. How many apples do they have each?

Grouping – 6 football stickers are shared between 2 people, how many do they each get?

Record on a vertical number line.

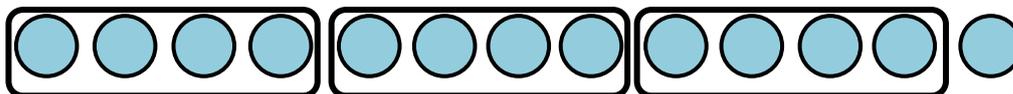
2 groups of 3

Count down from the highest number, arrows on the left of the number line. |

Children need to understand that this calculation reads as 'How many groups of 3 are there in 12?'

Children should also move onto calculations involving remainders.

$13 \div 4 =$



$13 \div 4 = 3 \text{ remainder } 1$

END OF YEAR 3 EXPECTATIONS:

Children will continue to use grouping (repeated subtraction) to represent their calculations, answering questions such as:

$24 \div 2 =$

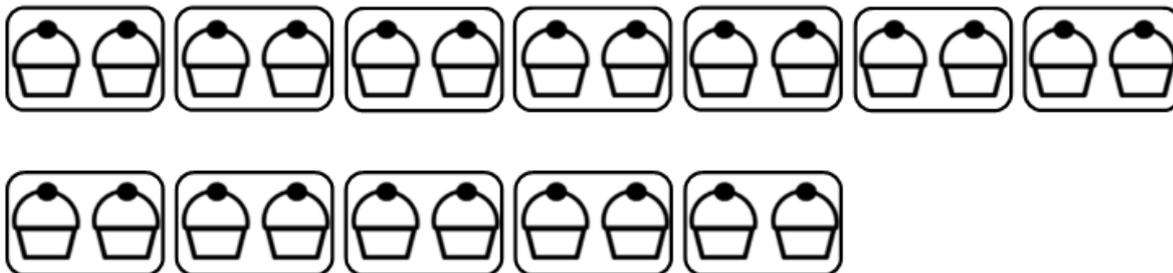
or

There are 24 cupcakes, how many people can have 2 cupcakes each?

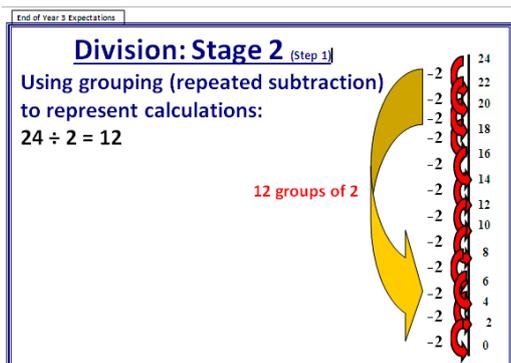


Mathematics Calculation Guidelines

Progression through Calculations for DIVISION



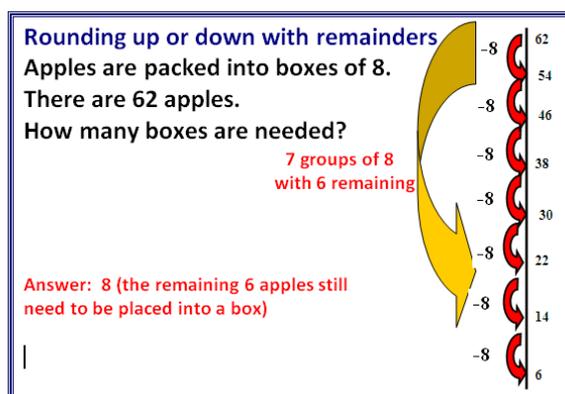
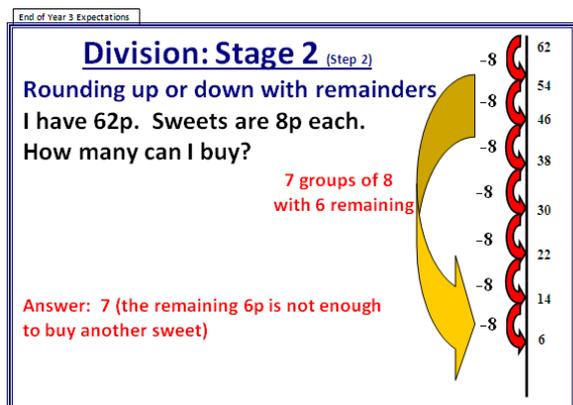
This should also be modelled alongside a **vertical** number line to emphasise that grouping is repeated subtraction.



Children need to be able to decide what to do with remainders after division and round up or down accordingly. They should make sensible decisions about rounding up or down after division. For example $62 \div 8$ is 7 remainder 6, but whether the answer should be rounded up to 8 or rounded down to 7 depends on the context.

E.g. I have 62p. Sweets are 8p each. How many can I buy?
Answer: 7 (the remaining 6p is not enough to buy another sweet)

Apples are packed into boxes of 8. There are 62 apples. How many boxes are needed?
Answer: 8 (the remaining 6 apples still need to be placed into a box)



END OF YEAR 4 EXPECTATIONS:

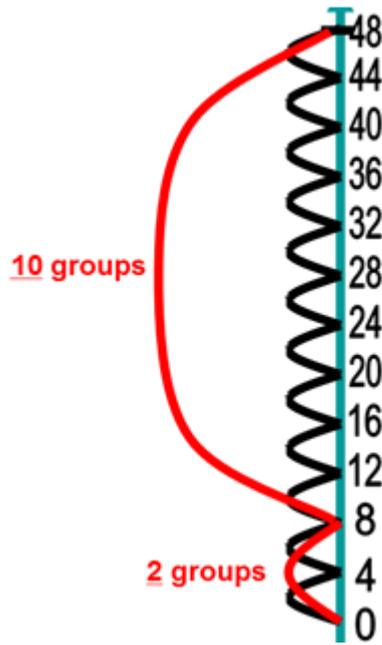
Before starting the more formal written method of 'chunking', children should be able to use the repeated subtraction on a vertical number line.

$$48 \div 4 = 12 \text{ (groups of 4)} \quad \text{leading to} \quad 48 \div 4 = 10 \text{ (groups of 4)} + 2 \text{ (groups of 4)} \\ = 12 \text{ (groups of 4)}$$



Mathematics Calculation Guidelines

Progression through Calculations for DIVISION



Children will develop their use of grouping (repeated subtraction) to be able to subtract multiples of the divisor, developing the use of the 'chunking' method.

Short division ($TU \div U$)

End of Year 4 Expectations

Division: Stage 3

Expanded vertical.

$$72 \div 3$$

3	72	<div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">10x</div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">10x</div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">4x</div>	Key Facts: 1 x 3 2 x 6 5 x 15 10 x 30
	- 30		
	42		
	- 30		
	12		
	- 12		
	0		

Answer: 24

Subtract larger multiples of the divisor

$$196 \div 6$$

6	196	<div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">30x</div> <div style="border: 1px solid black; border-radius: 50%; padding: 5px; display: inline-block;">2x</div>	Key Facts: 1 x 6 2 x 12 4 x 24 5 x 30 10 x 60 20 x 120
	- 180		
	16		
	- 12		
	4		

Answer: 32 remainder 4 or 32 r 4

Children should write key facts in a menu box. This will help them in identifying the largest group they can subtract in one chunk.

Children should write their answer above the calculation to make it easy for them and the teacher to distinguish.

Any remainders should be shown as integers, i.e. 32 remainder 4 or 32 r 4.



Mathematics Calculation Guidelines

Progression through Calculations for DIVISION

END OF YEAR 5 EXPECTATIONS:

Children can start to subtract larger multiples of the divisor (e.g. 20x).

Short division (HTU ÷ U)

$$196 \div 6$$

$$\begin{array}{r}
 32 \text{ r } 4 \\
 6 \overline{) 196} \\
 \underline{- 180} \\
 16 \\
 \underline{- 12} \\
 4
 \end{array}$$



1x	6
2x	12
4x	24
5x	30
10x	60
20x	120

The key facts in the menu box should be extended to include 4x and 20x.



Answer: 32 remainder 4 or 32 r 4

Any remainders should be shown as integers, i.e. 14 remainder 2 or 14 r 2.

Children need to be able to decide what to do after division and round up or down accordingly. They should make sensible decisions about rounding up or down after division. For example $240 \div 52$ is 4 remainder 32, but whether the answer should be rounded up to 5 or rounded down to 4 depends on the context.

Introduce shorter method 'Bus Stop Method' when children are ready.

End of Year 5 Expectations

Division: Stage 4.

Bus Stop Method

$37 \div 3$ can be modelled as:

$$\begin{array}{r}
 12 \text{ r } 1 \\
 3 \overline{) 37}
 \end{array}$$

$945 \div 7$ can be modelled as:

$$\begin{array}{r}
 135 \\
 7 \overline{) 945} \\
 \underline{23} \\
 945
 \end{array}$$

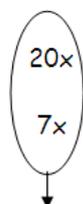
END OF YEAR 6 EXPECTATIONS:

Children may still use the menu box if required, but would also be expected to use larger multiples of the divisor (e.g. 20x, 30x, 40x).

Long division (HTU ÷ TU)

$$972 \div 36$$

$$\begin{array}{r}
 27 \\
 36 \overline{) 972} \\
 \underline{- 720} \\
 252 \\
 \underline{- 252} \\
 0
 \end{array}$$



Answer: 27



Mathematics Calculation Guidelines

Progression through Calculations for DIVISION

Any remainders should be shown as fractions, i.e. if the children were dividing 352 by 6, the answer should be shown as $58 \frac{4}{6}$ which could then be written as $58 \frac{2}{3}$ in its lowest terms.

This method should be extended to be used with decimals with up to two decimal places. Children should know that decimal points line up under each other.

e.g. $87.5 \div 7$

$$\begin{array}{r}
 12.5 \\
 7 \overline{) 87.5} \\
 \underline{- 70.0} \\
 17.5 \\
 \underline{- 14.0} \\
 3.5 \\
 \underline{- 3.5} \\
 0
 \end{array}$$

$10\times$
 $2\times$
 $0.5\times$

Answer: 12.5

End of Year 6 Expectations

Division: Stage 5.

Remainder expressed as fractions or decimal fractions

$676 \div 8 = 84.5$

$977 \div 36$ is approximately $1000 \div 40 = 25$

Include use of calculators to check.

Extension: $381 \div 16$

Answer: $23 \frac{13}{16}$

$16 \overline{) 381}$

$\underline{320} \text{ (16} \times 20\text{)}$

61

$\underline{48} \text{ (16} \times 3\text{)}$

13

By the end of year 6, children will have a range of calculation methods, mental and written. Selection will depend upon the numbers involved.

Children should not be made to go onto the next stage if:

- 1) they are not ready.
- 2) they are not confident.

Children should be encouraged to consider if a mental calculation would be appropriate before using written methods.